

## The Great Escape? A Quantitative Evaluation of the Fed's Liquidity Facilities<sup>†</sup>

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*We introduce liquidity frictions into an otherwise standard DSGE model with nominal and real rigidities and ask: can a shock to the liquidity of private paper lead to a collapse in short-term nominal interest rates and a recession like the one associated with the 2008 US financial crisis? Once the nominal interest rate reaches the zero bound, what are the effects of interventions in which the government provides liquidity in exchange for illiquid private paper? We find that the effects of the liquidity shock can be large, and show some numerical examples in which the liquidity facilities of the Federal Reserve prevented a repeat of the Great Depression in the period 2008–2009. (JEL E13, E31, E43, E44, E52, E58, G01)*

In December 2008, the federal funds rate collapsed to zero. Standard monetary policy through interest rate cuts had reached its limit. Around the same time, the Federal Reserve started to expand its balance sheet. By January 2009, the overall size of the Fed's balance sheet exceeded \$2 trillion, an increase of more than \$1 trillion compared to a few months earlier (Figure 1). This expansion mostly involved the Federal Reserve exchanging government liquidity (money or government debt) for private financial assets through direct purchases or collateralized short-term loans. These direct interventions in private credit markets were implemented via various facilities, such as the Term Auction Facility, the Primary Dealer Credit Facility, and

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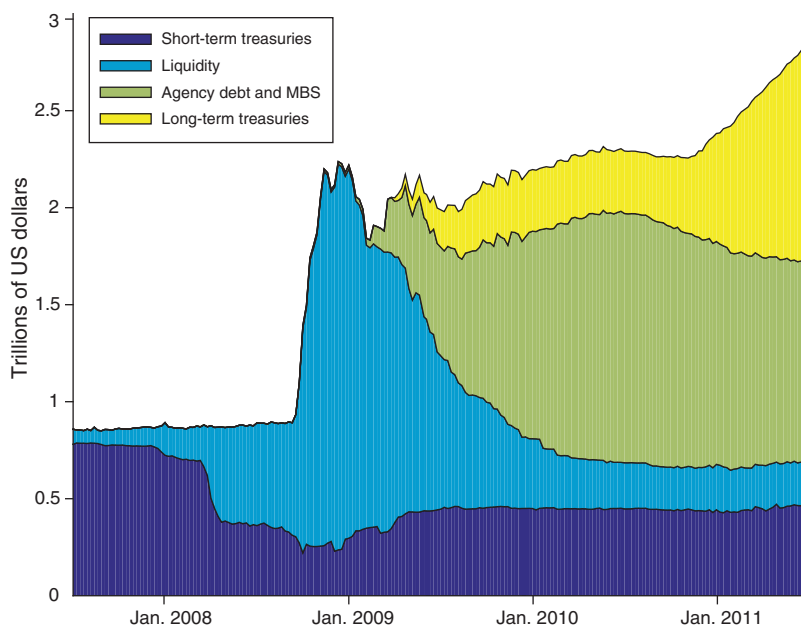


FIGURE 1. FEDERAL RESERVE'S ASSETS BETWEEN JULY 2007 AND JULY 2011

*Note:* The figure plots the evolution of the asset side of the Federal Reserve balance sheet between July 2007 and July 2011, decomposed in short-term Treasury securities, lending to financial institutions and liquidity to key credit markets, Agency debt and mortgage-backed securities, and long-term Treasury securities.

*Source:* Federal Reserve Bank of Cleveland

the Term Securities Lending Facility.<sup>1</sup> In broad terms, these facilities can be thought of as nonstandard open market operations, whereby the government exchanges highly liquid government paper for less liquid private paper. Alternatively, one can think of them as nonstandard discount window lending, which provides government liquidity—using private assets as collateral. This paper studies the quantitative effects of these liquidity policies on macroeconomic and financial variables.

Ever since the irrelevance result of Wallace (1981), the benchmark for many macroeconomists is that nonstandard open market operations in private assets are irrelevant. Eggertsson and Woodford (2003) show that this result extends to standard open market operations in models with nominal frictions and money in the utility function, provided that the nominal interest rate is zero. Once the nominal interest rate reaches its lower bound, liquidity has no further role in this class of models, or in most other standard models with various types of frictions, such as Rotemberg and Woodford (1997) or Christiano, Eichenbaum, and Evans (2005).

In this paper, we depart from such an irrelevance result by incorporating a particular form of credit frictions proposed by Kiyotaki and Moore (2012)—henceforth, KM. The KM credit frictions are of two distinct forms. First, a firm that faces an investment opportunity can borrow only up to a fraction of the value of its current

<sup>1</sup> See Armantier, Krieger, and McAndrews (2008); Adrian, Burke, and McAndrews (2009); Fleming, Hung, and Keane (2009); Adrian, Kimbrough, and Marchioni (2011); and Fleming and Klagge (2010) for details about the various facilities, and Madigan (2009) for a summary.

investment. This friction is a relatively standard financing constraint.<sup>2</sup> Second, a firm that faces an investment opportunity can sell only up to a certain fraction of the *illiquid* assets on its balance sheet in each period. In the model, these illiquid assets correspond to equity holdings of other firms. More generally, we interpret these illiquid assets as privately issued paper such as commercial paper, bank loans, mortgages, and so on. This friction is a less standard *resaleability* constraint.

In contrast to private assets, we follow KM and assume that government paper, i.e., money and bonds, is not subject to the resaleability constraint. This assumption gives government paper a primary role as liquidity. In this world, open market operations that change the composition of liquid and illiquid assets in the hands of the private sector affect the allocation of resources. The assumption of limited resaleability of private paper and the role of government paper as liquidity provide a natural story for the crisis of 2008 and the ensuing Fed's response. In our study, the source of the crisis of 2008 is a shock to the resaleability of private paper. Suddenly, secondary markets for private papers (such as privately issued mortgage-backed securities) froze. This shock led to a general decline of funding for investment and aggregate production through the interaction between the markets for assets, goods, and labor. We think of this propagation as capturing a central aspect of the crisis.

We embed the KM credit frictions in a relatively standard dynamic stochastic general equilibrium (DSGE) model along the lines of Christiano, Eichenbaum, and Evans (2005) and Smets and Wouters (2007). The model features nominal and real frictions, such as price and wage rigidities and aggregate capital adjustment costs. Conventional monetary policy is implemented via variations in the nominal interest rate according to a standard interest rate policy rule that is constrained by the zero bound. Nonconventional policy consists of open market operations in private assets that increase the overall level of liquidity in the economy. We use the expansion in the Fed's balance sheet after Lehman's bankruptcy to calibrate the nonstandard policy reaction function of the government.

Our main result is that both the financial shock and the liquidity policy can have a quantitatively large effect. A shock to the resaleability constraint, calibrated to match the increase in the premium associated with very liquid assets during the crisis (what Krishnamurthy and Vissing-Jorgensen 2012 call the "convenience yield"), accounts for more than one-half of the drop in output observed in the data and all of the drop in inflation. As a response, the nominal interest in the model hits the zero lower bound. The impact of the policy intervention is substantial. In our baseline scenario, absent nonstandard open market operations, output and inflation would have dropped by an additional 30 percent and 40 percent, respectively. Our quantitative results depend crucially on the expected duration of the crisis. Had private agents expected a more persistent freeze in the private paper market, the economy may have suffered a second Great Depression in the absence of interventions. With intervention, in some of our numerical examples, the economy "escapes" from a

<sup>2</sup>This constraint is similar to the collateral requirement in Kiyotaki and Moore (1997). Kocherlakota (2000) and Cordoba and Ripoll (2004) argue that collateral constraints have a limited quantitative role in explaining macroeconomic fluctuations. This result is, however, conditional on the fundamental shocks that drive the business cycle. Liu, Wang, and Zha (2013) and Nezafat and Slavik (2010) show that financial constraint do amplify the effects of shocks that shift the demand of collateral, capable of generating fluctuations of asset prices and aggregate production observed in data.

repeat of the Great Depression (hence, the title of the paper). The reason is that liquidity policies can have especially large effects at zero interest rates—a result reminiscent of the case of the multiplier of government spending in Eggertsson (2011) and Christiano, Eichenbaum, and Rebelo (2011).

Nominal rigidities and the zero lower bound (ZLB) on nominal interest rates play a crucial role in our analysis. Under flexible prices, the KM financial frictions can only account for a drop in investment. In this case, aggregate output is almost unchanged because consumption makes up for the fall in investment. The consumption boom requires the real interest rate to fall in order to induce people to spend more. Thus, the real rate of interest on liquid paper absent nominal frictions—the so-called natural rate of interest—needs to fall substantially. Furthermore, the loss of liquidity of private paper drives up the premium people are willing to pay for holding liquid government paper. This additional channel leading to a decline in the natural rate of interest during financial stress is absent in standard DSGEs.<sup>3</sup> But the actual real interest rate can hardly fall if the nominal interest rate cannot turn negative and prices are sluggish. As a consequence the freeze in the private paper market triggers a drop not only in investment, but also in consumption and aggregate output.

Unconventional policy can alleviate the crisis by targeting directly the source of the problem, which is the loss of liquidity of private paper. By swapping partially illiquid private paper for government liquidity, thus making the aggregate portfolio holdings of the private sector more liquid, the intervention lubricates financial markets, reducing the fall in investment and consumption. Importantly, we are not assuming that the policy intervention violates the private sector resaleability constraint. Instead, the intervention only increases the supply of government paper by purchasing private paper in the open market.

Our paper belongs to the strand of literature that studies the effect of financial disturbances in monetary DSGE models, such as Bernanke, Gertler, and Gilchrist (1999); Christiano, Motto, and Rostagno (2003, 2014); Goodfriend and McCallum (2007); and Curdia and Woodford (2010, 2015), among many others, and is particularly close to the papers by Ajello (2016); Gertler and Karadi (2011); and Gertler and Kiyotaki (2010).<sup>4</sup> What distinguishes our paper from the rest of the literature is both the friction and the nature of the shock. Ajello constructs a model featuring resaleability constraints as in KM, estimated using standard US macro time series and a measure of financial spreads. His main finding is that financial intermediation shocks are key drivers of business cycles and played a large role during the Great Recession. One important difference with our work is that the exogenous financial shock in Ajello affects the intermediation technology as in Curdia and Woodford (2015). As such, this shock would have an effect on the economy even in absence of

<sup>3</sup>Fisher (2015) and Anzoategui et al. (2016) analyze the fall of the natural rate by assuming that the household derives utility from holding Treasuries that show up in the utility function, building on Krishnamurthy and Vissing-Jorgensen (2012).

<sup>4</sup>The work of Gârleanu and Pedersen (2011) and Ashcraft, Gârleanu, and Pedersen (2011) on the implications of margin requirements is also very related to ours. Margin requirements represent a constraint on the agents' ability to leverage when buying assets. An increase in the shadow value of the constraints, which captures a funding-liquidity crisis, is akin to a liquidity shock in our model, in that it causes a sharp drop in investment and an increase of the spread between high-margin (illiquid) and low-margin (liquid) assets. These authors also study the effect of the liquidity facilities. Both papers mainly focus on the asset pricing implications of margin constraints and liquidity crisis, and have limited quantitative implications for macroeconomic variables.

resaleability constraints, and hence bears more resemblance to the exogenous component of spreads in the model of Bernanke, Gertler, and Gilchrist (1999) than to the liquidity shock in KM. Furthermore, Ajello investigates neither the importance of the liquidity facilities nor the role of the ZLB, which are at the center of our analysis.

Gertler and Karadi (2011) and Gertler and Kiyotaki (2010) have also analyzed the role of nonconventional central bank policies during the Great Recession. The key difference with our paper is that in our model the source of the disturbance is financial, while in these other papers the recession is triggered by a real shock. Specifically, we characterize the crisis as a reduction in the resaleability of private paper—a drying up of liquidity in the secondary markets for privately issued securities in the spirit of Gorton and Metrick (2010, 2012)—which in turn triggers the underutilization of the factors of production. In contrast, in Gertler and Karadi (2011) and Gertler and Kiyotaki (2010), the shock that triggers a recession is an exogenous reduction in the quality of the capital stock. Our shock need not imply any reduction in output if the existing capital and labor were utilized at the same rate as precrisis. It is the interaction of the financial and nominal frictions, and the inability of the central bank to accommodate this shock due to the ZLB, that gives rise to our account of the crisis. Also, in these papers the intervention subsidizes financial intermediaries and improves their balance sheet by preventing asset prices from falling significantly. In our model the liquidity interventions are not a subsidy to financial intermediaries. In fact, the government “makes money” via the intervention, at least in expectations, as it did *ex post* in the financial crisis.

Our main focus is on the Great Recession, which according to the National Bureau of Economic Research dates, began in December 2007 and ended in June 2009, with the focal point being the default of Lehman Brothers in September 2008. Although the market for mortgage-backed securities stopped working well in August 2007, our paper concentrates on the events that followed the default of Lehman Brothers. The Fed facilities that we evaluate in this paper were started in December 2007 and were escalated with the collapse of Lehman in the fall of 2008, when the Fed funds rate ultimately reached zero.<sup>5</sup>

Before going further, we should emphasize a few important limitations of our analysis. The liquidity constraints proposed by KM are reduced form. Recently, Kurlat (2013) and Bigio (2015) have shown that these liquidity constraints can arise endogenously in a model in which entrepreneurs have asymmetric information about the quality of existing assets.<sup>6</sup> An advantage of taking a reduced-form approach is that one does not have to take a stand on the specific mechanism behind the fall in liquidity in financial markets, whether due to asymmetric information or sunspots.<sup>7</sup>

<sup>5</sup>Our analysis does not extend to the large-scale asset purchase program implemented during the fall of 2010 in response to the further weakening of economic activity, because this quantitative easing program (at least when implemented via purchases of long-term Treasuries) involves swapping one liquid asset for another type of liquid asset. The *preferred habitat theory* (studied in Vayanos and Vila 2009, and in Chen, Curdia, and Ferrero 2012 in the context of an estimated DSGE model) can provide a rationale for this type of asset purchase program.

<sup>6</sup>In Kurlat (2013), for instance, markets for existing assets can shut down as a consequence of large enough investment-specific productivity shocks. More generally, the combination of shocks to fundamentals and adverse selection can induce large drops of price and trading volume in secondary markets. Cui and Radde (2014) construct a model in which private papers are traded subject to matching frictions in which shocks to the matching efficiency change the resaleability of private papers endogenously.

<sup>7</sup>One interpretation of our shock to the resaleability constraint is that the economy switches from a high resaleability to a low resaleability equilibrium due to *sunspots*, i.e., without a change of the other fundamentals.

The cost is that our model is silent on whether the Fed's interventions can affect the incentive structure of the private sector. This aspect is certainly important, as the private sector response may lead to an endogenous change in the liquidity constraints that we currently take as given. More generally, we abstract from the costs of intervening, which can take many different forms. Therefore, our paper has only positive, not normative, content: we show that liquidity interventions can be quantitatively important for macroeconomic stability in the short run. Our findings suggest that understanding the consequences of these policies for the incentives of the private sector should be a high priority on the research agenda.

Sections I and II describe the model and its calibration. Section III discusses the results, and Section IV concludes.

## I. The Model

The model can be described as KM augmented with both nominal and real frictions. The economic actors in the model are households, whose members are entrepreneurs and workers, the government, intermediate and final goods firms, labor agencies, and capital producers.

### A. Households

The economy is populated by a continuum of identical households of measure one. Each household consists of a continuum of members indexed by  $j \in [0, 1]$ . In every period, household members receive an i.i.d. draw that determines whether they are entrepreneurs or workers. The probability of being an entrepreneur is  $\varkappa$ , which, by the law of large numbers, is also the fraction of entrepreneurs in the household. Each entrepreneur  $j \in [0, \varkappa)$  has an opportunity to invest but does not work. Each worker member  $j \in [\varkappa, 1]$  supplies differentiated labor of type  $j$  but does not invest.<sup>8</sup> The friction in our model described below affects the transfer of funds from those who do not have an investment opportunity (the workers) to those who do (the entrepreneurs).

Let  $C_t(j)$  denote the amount of the consumption good each member of the household purchases in the market place in period  $t$ . An assumption of the representative household structure is that, at the end of the period, all members bring the consumption purchases back to the household, and these goods get distributed equally among all members. Utility thus depends upon the sum of all the consumption goods bought by the different household members,

$$(1) \quad C_t \equiv \int_0^1 C_t(j) dj.$$

<sup>8</sup> Although each member randomly becomes an entrepreneur or a worker, we renumber household members every period so that a member  $j \in [0, \varkappa)$  is an entrepreneur and a member  $j \in [\varkappa, 1]$  is a worker who supplies type- $j$  labor. The original KM model features heterogeneity. Each entrepreneur occasionally receives an opportunity to invest while workers never do. Aggregation is obtained by imposing a few additional assumptions. In this paper, we adopt a modified version of the KM model based on Shi (2015), which is more amenable to modifications, allowing us to perform a more extensive sensitivity analysis.

Let  $H_t(j)$  be hours worked by worker member  $j$ . The household’s objective is

$$(2) \quad E_t \sum_{s=t}^{\infty} \beta^{s-t} \left[ \frac{C_s^{1-\sigma}}{1-\sigma} - \frac{\omega}{1+\nu} \int_{\infty}^1 H_s(j)^{1+\nu} dj \right],$$

where  $\beta \in (0, 1)$  is the subjective discount factor,  $\sigma > 0$  is the coefficient of relative risk aversion,  $\nu > 0$  is the inverse of Frisch elasticity of labor supply, and  $\omega > 0$  is a parameter that pins down the steady-state level of hours. This construction of the representative household permits us to study a situation in which people face idiosyncratic investment opportunities, while at the same time retaining the tractability of the representative household structure, thus abstracting from consumption heterogeneity across different types of agents.

At the end of each period, the household also shares all the assets accumulated during the period among members. Entering the next period, therefore, each member holds an equal share of the household’s assets. An important assumption is that, after the idiosyncratic shock is realized and each member knows its type, the household cannot reshuffle the allocation of resources among its members. Instead, those household members who would like to obtain more funds need to seek the money from other sources. The assets available to household members are described in the table below, which summarizes the household’s balance sheet at the beginning of period  $t$  (before interest payments), expressed in terms of the consumption goods. Households own government-issued nominal bonds  $B_t$ , where  $P_t$  is the price level,  $K_t$  is physical capital, and  $N_t^O$  represents claims on other households’ capital. Households’ liabilities consist of claims on own capital sold to other households  $N_t^I$ , and net equity  $N_t$  is defined as

$$(3) \quad N_t = N_t^O + K_t - N_t^I.$$

Capital is homogeneous, earns per-unit rental income  $r_t^k$ , and has a unit value  $q_t$  in terms of consumption goods. A fraction  $\delta$  of capital depreciates in each period. Bonds pay a gross nominal interest rate  $R_t$ . Note that all households liabilities—all claims to the assets of the private sector in the model—are in the form of equity.

HOUSEHOLD’S BALANCE SHEET (*Tradable Assets*)

Assets		Liabilities	
Nominal bonds	$B_t/P_t$	Equity issued	$q_t N_t^I$
Others’ equity	$q_t N_t^O$		
Capital stock	$q_t K_t$	Net worth	$q_t N_t + B_t/P_t$

The owner of capital receives the rental income as well as profits of intermediate goods producers and capital goods producers as dividend in proportion of capital ownership.<sup>9</sup> Define per-period real profits of all the intermediated goods producers

<sup>9</sup>Here we consider an economy in which equity holders receive the returns from all the fixed factors of production, including physical capital, intangible capital (knowledge and patent to produce differentiated goods), and

and capital good producers as  $D_t = \int_0^1 D_t(i) di$  and  $D_t^I$ , respectively. The dividend per unit of capital ownership is

$$R_t^k = r_t^k + \frac{D_t + D_t^I}{K_t}.$$

Finally, households pay lump-sum taxes  $\tau_t$  to the government.

During the operation of the market, members decide how to allocate their resources between purchases of the nonstorable consumption good, savings in the different assets, and, if entrepreneurs, investment in new capital. Those members who are workers also supply the hours demanded by firms at the wage contracted by the labor unions (as we shall see, workers have some monopolistic power and wages are sticky) and can therefore include their salaries among the available resources. Specifically, each household member’s flow of funds is

$$(4) \quad C_t(j) + p_t^I I_t(j) + q_t [N_{t+1}(j) - I_t(j)] + \frac{B_{t+1}(j)}{P_t} \\ = [R_t^k + (1 - \delta) q_t] N_t + \frac{R_{t-1} B_t}{P_t} + \frac{W_t(j)}{P_t} H_t(j) - \tau_t,$$

where  $H_t(j) = 0$  for entrepreneurs ( $j \in [0, \varkappa)$ ) and  $I_t(j) = 0$  for workers ( $j \in [\varkappa, 1]$ ),  $W_t(j)$  is the nominal wage for type- $j$  labor, and  $p_t^I$  is the price of new capital in terms of the consumption good, which differs from 1 due to capital adjustment costs.

Most of the action in the model is a consequence of the financial frictions, which translate into constraints on the financing of new investment projects by entrepreneurs and on the evolution of the balance sheet.<sup>10</sup> The key frictions proposed by KM that we adopt here are of two forms. First, a *borrowing constraint* implies that any entrepreneur can only issue new equity up to a fraction  $\theta$  of her investment. Second, a *resaleability constraint* implies that in any given period a household member can sell only a fraction  $\phi_t$  of her existing equity holdings. An important simplification in KM is that the equity issued by the other households is a perfect substitute for the equity position in the household’s own business (capital stock minus equity issued) and thus subject to exactly the same resaleability constraint.<sup>11</sup> As a consequence, the borrowing constraint and the two resaleability constraints (on claims on capital

the fixed factor to limit investment goods production. Hall (2001) argues that intangible capital is essential for understanding stock market fluctuations.

<sup>10</sup>These frictions are also front and center in the original KM formulation. We assume a slightly different asset market structure in which government-issued paper in general, rather than just money (effectively a *bubble asset*), serves as the liquid asset and pays a nominal interest rate  $R_t$ . We make this assumption because we characterize conventional monetary policy in terms of nominal interest rate setting, as standard in the New Keynesian literature (e.g., Woodford 2003) and we study issues related to the ZLB.

<sup>11</sup>Thus, in addition to selling a fraction  $\phi_t$  of the equity holdings of the other households, each household can remortgage a fraction  $\phi_t$  of capital stock that has not been borrowed against previously. This simplification is essential for aggregation in KM. While not indispensable in our model with a representative household, we continue to use this assumption in order to simplify the algebra.



of other households and on claims on own capital) can be consolidated (see online Appendix B.4 for the explicit derivation) and written in terms of net equity  $N_t$  as

$$(5) \quad N_{t+1}(j) \geq (1 - \theta)I_t(j) + (1 - \phi_t)(1 - \delta)N_t.$$

The first part of the right-hand side of the inequality,  $(1 - \theta)I_t(j)$ , represents a constraint on borrowing to finance new investment for those agents who have an investment opportunity. If  $\theta$  were equal to 1, the entrepreneur would be able to finance the entire investment by selling equity in financial markets. When  $\theta < 1$ , the entrepreneur is forced to retain  $1 - \theta$  fraction of investment as own equity and use her own fund to partly finance the investment cost. The second part of the right-hand side,  $(1 - \phi_t)(1 - \delta)N_t$ , represents the resaleability constraint. In period  $t$ , household members can sell only a fraction  $\phi_t$  of their existing equity.

While literally  $\phi_t$  represents a restriction on transactions, we follow KM in interpreting changes in  $\phi_t$  as liquidity shocks. These shocks capture, in reduced form, changes in market liquidity. Alternatively,  $\phi_t$  can also be thought of as 1 minus the haircut in the repo market: a measure of how much liquidity entrepreneurs can obtain for \$1 worth of collateral. Under this interpretation, shocks to  $\phi_t$  would capture changes in funding conditions in the repo market.<sup>12</sup> The purpose of this paper is to investigate whether this shock alone can be responsible for the bulk of the Great Recession, and the extent to which unconventional policy was successful in mitigating the impact of this shock.

Another significant feature of the model is that the asset  $B_t$  is not subject to any resaleability constraint and is therefore liquid. Obviously, household members for whom constraint (5) is binding would like to acquire resources from the market by issuing liquid assets. We rule out this possibility by assuming that only the government can issue the liquid asset while households can only take a long position in it:

$$(6) \quad B_{t+1}(j) \geq 0.$$

Broadly speaking, we think of equity in the model as comprising all claims on private assets, which in reality take the form of equity or debt, while  $B_t$  represents any form of government paper. We abstract from private banks as separate agents who supply liquid paper. Instead, all private assets are partially liquid in the same measure, and all private agents serve as financial intermediaries by simultaneously providing funds for others' capital investment and raising funds for their own investment. Indeed, even the investing entrepreneurs continue providing funds to the other entrepreneurs due to the resaleability constraint. In an abstract way, the fall in resaleability corresponds to the disruption of the financial system.<sup>13</sup> The two constraints (5) and (6) are central to the analysis. The next section argues that, in equilibrium,

<sup>12</sup>Gorton and Metrick (2012) argue that a run on the repo market is at the origin of the collapse of financial markets in the fall of 2008.

<sup>13</sup>We assumed all the private paper is equity in our model. Even if some private papers were debt, because all members are identical ex ante, each member's private net debt position would be zero at the beginning of the period. Thus, the equilibrium would not change unless we change the borrowing and resaleability constraints. This consideration is behind the idea of using of yield spreads between Treasury bonds and private bonds in zero net aggregate supply to calibrate the time series of liquidity in the next section.

both constraints are binding for entrepreneurs and studies the consequences for the household decision problem as a whole.

At the end of the period, household equity, bond holdings, and capital are given, respectively, by

$$\begin{aligned}
 (7) \quad N_{t+1} &= \int N_{t+1}(j) dj, \\
 (8) \quad B_{t+1} &= \int B_{t+1}(j) dj, \\
 (9) \quad K_{t+1} &= (1 - \delta) K_t + \int I_t(j) dj.
 \end{aligned}$$

We now move to the actual decisions of each type of household member. An important assumption is that each member of the household acts in the interest of the whole family.

*Entrepreneurs.*—The flow of funds for entrepreneur  $j \in [0, \varkappa)$  is given by expression (4), with  $H_t(j) = 0$ . That constraint clarifies that, as long as the market price of equity  $q_t$  is greater than the price of newly produced capital  $p_t^I$ , entrepreneurs trying to maximize the household’s utility will use all available resources to create new capital. In the rest of the paper, we focus on constrained equilibria in which the condition  $q_t > p_t^I$  is satisfied.<sup>14</sup> In these equilibria, entrepreneurs sell all holdings of government bonds because the expected return on new investment dominates the return on the liquid asset. Furthermore, the entrepreneur also sells as much existing equity as possible and issues the maximum amount of new equity to take full advantage of the investment opportunity. As a consequence, the constraints arising from financial frictions (5) and (6) are both binding, and entrepreneurs spend no resources on consumption goods:

$$\begin{aligned}
 (10) \quad N_{t+1}(j) &= (1 - \theta)I_t(j) + (1 - \phi_t)(1 - \delta) N_t(j), \\
 (11) \quad B_{t+1}(j) &= 0, \\
 (12) \quad C_t(j) &= 0,
 \end{aligned}$$

for  $j \in [0, \varkappa)$ .<sup>15</sup>

Substituting (10) through (12) into the flow of funds (4) and setting  $H_t(j) = 0$ , we obtain the amount of investment by each entrepreneur:

$$(13) \quad I_t(j) = \frac{[R_t^k + (1 - \delta) q_t \phi_t] N_t + \frac{R_{t-1} B_t}{P_t} - \tau_t}{p_t^I - \theta q_t}.$$

<sup>14</sup>We first ensure that the condition  $q_t > p_t^I$  holds at steady state, and then check that it is satisfied in our numerical experiments.

<sup>15</sup>Since entrepreneurs are constrained and the consumption good is jointly consumed at the end of the period, it is optimal for workers to buy all the consumption goods, directing all of the liquidity of entrepreneurs to investment.

Therefore, aggregate investment in the economy equals

$$(14) \quad I_t = \int_0^{\varkappa} I_t(j) dj = \varkappa \frac{[R_t^k + (1 - \delta) q_t \phi_t] N_t + \frac{R_{t-1} B_t}{P_t} - \tau_t}{p_t^I - \theta q_t}.$$

The denominator represents the liquidity needs for one unit of investment—the gap between the investment goods price and the amount the entrepreneur can finance by issuing equity ( $\theta q_t$ ). The numerator measures the amount of liquidity available to entrepreneurs. Clearly, a drop in  $\phi_t$  reduces the amount of liquidity available to finance investment.<sup>16</sup>

*Workers.*—The flow of funds for worker  $j \in [\varkappa, 1]$  is given by expression (4), with  $I_t(j) = 0$ . Workers do not choose hours directly. Rather, the union who represents each type of worker member sets wages on a staggered basis. As a consequence, the household supplies labor as demanded by firms at the posted wages.

In order to find the workers' decisions in terms of asset and consumption choices, we derive the household's decisions for  $N_{t+1}$ ,  $B_{t+1}$ , and  $C_t$  as a whole, taking wages and hours as given. Since we know the solution for entrepreneurs from the last section (that is,  $N_{t+1}(j)$ ,  $B_{t+1}(j)$ , and  $C_t(j)$  for  $j \in [0, \varkappa)$ ), constraints (1), (7), and (8) determine  $C_t(j)$ ,  $N_{t+1}(j)$ , and  $B_{t+1}(j)$  for workers. We then check that these choices satisfy the financing constraints (5) and (6) for workers.

The aggregation of workers' and entrepreneurs' budget constraints yields

$$(15) \quad C_t + p_t^I I_t + q_t(N_{t+1} - I_t) + \frac{B_{t+1}}{P_t} = [R_t^k + (1 - \delta) q_t] N_t + \frac{R_{t-1} B_t}{P_t} + \int_{\varkappa}^1 \frac{W_t(j) H_t(j)}{P_t} dj - \tau_t.$$

Households choose  $C_t$ ,  $N_{t+1}$ , and  $B_{t+1}$  in order to maximize utility (2) subject to (14) and (15). As long as  $q_t > p_t^I$ , the first-order conditions for bonds and equity are, respectively,

$$(16) \quad C_t^{-\sigma} = \beta E_t \left\{ C_{t+1}^{-\sigma} \frac{R_t}{\pi_{t+1}} \left[ 1 + \frac{\varkappa(q_{t+1} - p_{t+1}^I)}{p_{t+1}^I - \theta q_{t+1}} \right] \right\},$$

where  $\pi_t$  is the gross inflation rate, and

$$(17) \quad C_t^{-\sigma} = \beta E_t \left\{ C_{t+1}^{-\sigma} \left[ \frac{R_{t+1}^k + (1 - \delta) q_{t+1}}{q_t} + \frac{\varkappa(q_{t+1} - p_{t+1}^I)}{p_{t+1}^I - \theta q_{t+1}} \right] \times \frac{R_{t+1}^k + (1 - \delta) \phi_{t+1} q_{t+1}}{q_t} \right\}.$$

<sup>16</sup>The entrepreneurs should not be thought of as the same characters populating the entrepreneurship literature in macroeconomics (see Quadrini 2009 for an extensive review). Instead, entrepreneurs here are best thought of as capturing the broad functions of financial markets, funneling resources from savers to the production sector of the economy. The key friction in the model consists of an impediment to this *funneling*, which intensifies in the event of a financial crisis.

Equations (14), (16), and (17) describe the household’s choice of investment, consumption, and portfolio for a given price process.

The payoff from holding paper, either bonds or equity, consists of two parts. The first is the standard return:  $\frac{R_t}{\pi_{t+1}}$  for bonds and  $\frac{R_{t+1}^k + (1 - \delta) q_{t+1}}{q_t}$  for equity. The second is the premium associated with the fact that this paper, when in the hand of entrepreneurs, relaxes their investment constraint. The value of this premium is  $\frac{\varkappa(q_t - p_t^I)}{p_t^I - \theta q_t}$ . The quantity  $\frac{\varkappa}{p_t^I - \theta q_t}$  measures the increase in investment afforded by an extra dollar of liquidity, where  $\varkappa$  and  $\frac{1}{p_t^I - \theta q_t}$  capture the fraction of liquidity going to entrepreneurs and the extent to which the investment increases by an extra unit of liquidity, respectively. The magnitude  $q_t - p_t^I$  measures the marginal value to the household of acquiring capital. The larger the difference between  $q_t$  and  $p_t^I$ , the more valuable for the household to acquire capital by investing and pay  $p_t^I$  per unit, rather than pay  $q_t$  on the market. This premium for liquidity applies to the entirety of bond returns, but only to the liquid part of the equity return  $\frac{R_{t+1}^k + (1 - \delta) \phi_{t+1} q_{t+1}}{q_t}$ , if  $\phi_{t+1}$  is less than 1. Hence, equity pays a premium in the expected rate of return relative to bonds because of its lower liquidity.

### B. The Convenience Yield

At the heart of our model is the idea that government paper is more liquid than privately issued papers: agents are willing to pay a premium for holding Treasuries—what Krishnamurthy and Vissing-Jorgensen (2012)—henceforth, KJVJ—call the *convenience yield*. In our model the convenience yield arises because liquid assets relax the financing constraint in the next period. It is then natural to define it as

$$(18) \quad CY_t \equiv E_t \left[ \frac{\varkappa(q_{t+1} - p_{t+1}^I)}{p_{t+1}^I - \theta q_{t+1}} \right],$$

where  $\frac{\varkappa(q_{t+1} - p_{t+1}^I)}{p_{t+1}^I - \theta q_{t+1}}$  is the premium due to the relaxation of the investment constraint.

Because what we observe in financial markets are spreads, we find it convenient in terms of our calibration described below to express  $CY_t$  as a spread. As shown above, the gross nominal interest rate  $R_t$  on a perfectly liquid one-period Treasury security satisfies Euler equation (16). The Euler equation for an otherwise identical security offering no convenience services is<sup>17</sup>

$$(19) \quad C_t^{-\sigma} = \beta E_t \left\{ C_{t+1}^{-\sigma} \frac{R_t^0}{\pi_{t+1}} \right\},$$

where  $R_t^0$  is its gross nominal interest rate. The spread between these two securities is given by

$$\overline{CY}_t = [R_t^0 - R_t] E_t \left( \frac{1}{\pi_{t+1}} \right).$$

<sup>17</sup>Imagine this illiquid bond repays to the holder at the end of the next period. It is too late for the bond holder to finance investment even though it is not late for consumption. In our model we assume that these securities are in small enough supply that they can be ignored. Nonetheless we can price them.

We show in online Appendix B.7 that  $\overline{CY}_t$  is approximately equal to  $CY_t$ .<sup>18</sup>

### C. Final and Intermediate Good Firms, Capital Producers, and Labor Markets

The remainder of the production side is standard along the lines of Christiano, Eichenbaum, and Evans (2005) and Smets and Wouters (2007). We refer the details to online Appendices B.1 through B.3, and sketch the framework below. Perfectly competitive final good producers combine intermediate goods,  $Y_{it}$ , to sell a homogeneous final good  $Y_t$  to households and capital producers. Each intermediate good producer pays a fixed cost, and hires capital and a composite labor to produce output. Facing a downward-sloping demand curve with monopoly power parameter  $\lambda_p$  for its product, each producer sets its price on a staggered basis, where  $1 - \xi_p$  is the probability of resetting the price in each period. As in Erceg, Henderson, and Levin (2000), we introduce wage rigidities assuming labor unions represent each type of imperfectly substitutable labor inputs  $H_t(j)$ , which are combined into a homogeneous composite sold to the intermediate firms. Facing a downward-sloping demand curve with monopoly power  $\lambda_w$ , each union sets the wage of each type of labor on a staggered basis so that in each period a new wage is set for a particular type of labor with probability  $1 - \xi_w$ . Finally, perfectly competitive capital producers produce investment goods, sold to the entrepreneurs at price  $p_t^I$ , under decreasing returns to scale technology. The total cost of producing  $I_t$  investment goods equals  $I_t[1 + S(I_t/I)]$ , where  $I$  is investment in steady state. We assume  $S(1) = S'(1) = 0$  and  $S''(I_t/I) > 0$  so that the price of investment goods differs from the price of consumption goods in the short run.

### D. The Government

The government conducts conventional monetary policy, unconventional credit policy, and fiscal policy. Conventional monetary policy consists of the central bank setting the nominal interest rate following a standard feedback rule subject to the ZLB:

$$(20) \quad R_t = \max \left\{ R \pi_t^{\psi_\pi} \left( \frac{Y_t}{\bar{Y}} \right)^{\psi_y}, 1 \right\},$$

where  $\psi_\pi > 1$  and  $\psi_y > 0$ . Unconventional credit policy corresponds to government purchases of private paper (denoted by  $N_{t+1}^g$ ) as a function of its liquidity

$$(21) \quad N_{t+1}^g = \psi_k(\phi_t - \phi),$$

where  $\psi_k < 0$ . Rule (21) captures the behavior of the Federal Reserve in terms of the liquidity facilities, as shown in Figure 1. According to this rule, the government intervenes when the liquidity of private paper is abnormally low. When the liquidity returns to normal, the facilities are discontinued. Since we consider a crisis state as

<sup>18</sup> Online Appendix B.7 shows how the convenience yield is related to the yield spread between a pair of longer maturity zero-coupon bonds, one perfectly liquid and the other perfectly illiquid.

low resaleability  $\phi_t$  state, we believe that this description of the intervention captures the behavior of the Fed during the financial crisis of 2008. We calibrate the parameter  $\psi_k$  to deliver a balance sheet increase in line with the data.

We stress that the government intervenes in the open market. Therefore, the intervention does not directly relax any agents' resaleability constraint (5).<sup>19</sup> The intervention affects macroeconomic outcomes by changing the *aggregate* portfolio composition of the private sector, skewing it toward liquid assets. Therefore, even if the economy is subject to a liquidity shock, entrepreneurs can muster resources to finance investments (see expression (14)). In the first period, the portfolio composition of the private sector is predetermined, however. Hence, on impact, the intervention is effective only via its impact on expectations and prices.

The government budget constraint is

$$(22) \quad q_t N_{t+1}^g + \frac{R_{t-1} B_t}{P_t} = \tau_t + [R_t^k + (1 - \delta) q_t] N_t^g + \frac{B_{t+1}}{P_t}.$$

The government purchase of equity and debt repayment is financed by a net tax (primary surplus), returns on equity holdings, and the new debt issuances. We assume that the government ensures intertemporal solvency by following a fiscal rule, written in deviations from steady state, according to which net taxes are proportional to the beginning-of-period government net debt position:

$$(23) \quad \tau_t - \tau = \psi_\tau \left[ \left( \frac{R_{t-1} B_t}{P_t} - \frac{RB}{P} \right) - q_t N_t^g \right],$$

where  $\psi_\tau > 0$ , and where  $\tau$  and  $\frac{RB}{P}$  are steady-state taxes and beginning-of-period government debt, respectively (the steady-state value of  $N_t^g$  is zero by assumption). Because the adjustment of taxes to debt is gradual (to the extent that  $\psi_\tau$  is small), the government has to finance emergency private paper purchases almost entirely by issuing debt.

### E. Equilibrium and Solution Strategy

In equilibrium, households and firms maximize their objectives subject to their constraints. Aggregate capital evolves according to

$$K_{t+1} = (1 - \delta) K_t + I_t,$$

where the capital stock is owned by either households or government according to

$$K_{t+1} = N_{t+1} + N_{t+1}^g.$$

Finally, the aggregate resource constraint requires that

$$Y_t = C_t + \left[ 1 + S \left( \frac{I_t}{Y_t} \right) \right] I_t.$$

<sup>19</sup>Hence, our policy intervention is somewhat different from that in Ashcraft, Gârleanu, and Pedersen (2011), where the government directly relaxes the margin requirements.

We consider an economy in which the liquidity constraints are always binding. A formal definition of the equilibrium, with a detailed list of the set of equations, is relegated to the online Appendix. We assume  $\phi_t$  follows a stationary AR(1) process, and consider a crisis as a large negative shock to  $\phi_t$ . Specifically, we assume that a large negative shock to  $\phi_t$  unexpectedly hits the economy at time  $t$ , starting from a steady state in period  $t - 1$ , and that no more shocks occur afterward. We use a Newton-Raphson algorithm to examine the nonlinear perfect foresight path, taking into account that the nominal interest rate may be constrained endogenously by the zero bound in the early stage.<sup>20</sup>

## II. Calibration

We calibrate the model at quarterly frequency and use a postwar/pre-Great Recession sample (1953:I–2008:III) in the United States to compute our targets. Table 1 shows the calibrated values of the parameters.

### A. Steady-State Parameters

The centerpiece of our calibration strategy for the parameters characterizing the degree of steady-state financial frictions is based on the work of KVJ, who provide us with an empirical estimate of the convenience yield. Specifically, KVJ model the convenience yield as a piecewise linear function  $b_1 \max\left\{b_2 - \frac{B}{PY}, 0\right\}$ , and estimate  $b_1$  and  $b_2$  (in their regression  $\frac{B}{PY}$  is measured by the ratio of Treasuries over GDP). Also in our model  $CY_t$  depends on the supply of liquid assets. In fact, KVJ's functional form is consistent with our framework: as the amount of liquidity in the economy increases, the liquidity premium drops because the entrepreneurs' constraint become less binding. After some threshold  $\frac{B}{PY}$ , the constraint is no longer binding,  $q$  drops to 1 (the steady-state value of  $p^l$ ),  $K$  approaches the efficient level, and the convenience yield becomes 0.

Figure 2 shows that the model can replicate the results of the KVJ's regressions shown in the first two columns of Table 3 of their paper and reproduced by the dashed lines.<sup>21</sup> The solid line plots the convenience yield in the model as a function of  $\frac{B}{PY}$ .<sup>22</sup> The average value of  $\frac{B}{PY}$  in our sample, which is 40 percent and is indicated by the vertical line in Figure 2, implies a steady-state convenience yield of 0.455 percent.<sup>23</sup>

<sup>20</sup>We implement the solution by using Dynare. We have also experimented with several other solution methods, such as the two-state stochastic Markov process approach in Eggertsson (2008), which uses perturbation methods, in earlier variations of the paper, finding similar results. The current approach has the advantage of capturing the full nonlinear dynamics of the model, although at the expense of abstracting from uncertainty.

<sup>21</sup>The two regressions are from slightly different samples. We chose to replicate the results in column 2 (the sample closest to ours) but the two sets of coefficients are very close.

<sup>22</sup>Two comments are in order. First, since KVJ's regressions are obtained using annual data and capture secular movements in the liquidity premium, we compute the mapping between liquidity  $\frac{B}{PY}$  and the convenience yield using the steady-state relationships. Second, because KVJ use spreads to measure the convenience yield, we use  $\overline{CY}$  as opposed to  $CY$  (see Section IB) in computing this mapping. Online Appendix B.7 shows that at steady state  $\overline{CY}$  and  $CY$  are the same regardless of the maturity of the security.

<sup>23</sup>In order to be consistent with KVJ, we measure  $\frac{B}{PY}$  as the amount of Treasury securities relative to GDP. If we adopt the notion of liquid assets in the hands of the public used in the construction of the liquidity share (essentially

TABLE 1—PARAMETERS

<i>Steady-state parameters</i>						
$\phi$ Resaleability constraint	$\theta$ Borrowing constraint	$\beta$ Discount factor	$\chi$ Probability of investment opportunity	$\delta$ Depreciation rate	$\gamma$ Capital share	$\frac{B/P}{4Y}$ Annualized s.s. liquidity
0.309	0.792	0.993	0.009	0.024	0.340	0.400
<i>Parameters characterizing the dynamics</i>						
$\sigma$ Relative risk aversion	$\nu$ Inverse Frisch elasticity	$S''(1)$ Investment adjustment cost	$\zeta_p$ Price Calvo probability	$\zeta_w$ Wage Calvo probability	$\lambda_p$ Price s.s. markup	$\lambda_w$ Wage s.s. markup
1.000	1.000	0.750	0.750	0.750	0.100	0.100
$\psi_\pi$ Taylor rule inflation response	$\psi_y$ Taylor rule output response	$\psi_\tau$ Tax rule response				
1.500	0.125	0.100				
<i>Liquidity shock and policy response</i>						
Baseline			Great escape			
$\Delta\phi$ Size of liquidity shock (percent log change)	$\rho_\phi$ Shock persistence	$\psi_k$ Policy intervention	$\Delta\phi$ Size of liquidity shock	$\rho_\phi$ Shock persistence	$\psi_k$ Policy intervention	
-0.218	0.953	-4.801	same	0.984	same	

Notes: The table shows the parameter values of the model for the baseline calibration. The last row also reports the size and the persistence of the shock, and the coefficient in the government rule for purchases of private assets in the Great Escape calibration.

The three parameters that characterize the degree of financial frictions in the model are  $\theta$  (the borrowing constraint),  $\phi$  (the resaleability constraint), and  $\chi$  (the fraction of entrepreneurs). These parameters directly affect the tightness of the financing constraint in the steady state. Replicating the two-piece linear KVJ regression provides two targets for the calibration: the steady-state convenience yield and the threshold  $\frac{B}{PY}$ . An additional target is provided by the average liquidity share in our sample, defined as

$$(24) \quad LS_t = \frac{B_{t+1}}{B_{t+1} + P_t q_t K_{t+1}}.$$

The liquidity share provides indirect evidence on the value of capital  $q$ , and hence on the stringency of financial constraints. As the financing constraint gets tighter with smaller  $\theta$ ,  $\phi$ , and  $\chi$ , the gap between  $q$  and one (the steady-state value of  $p^I$ ) expands for a given supply of government liquid asset  $B/PY$ , and the liquidity share drops (see Figure A-5 in the online Appendix). We construct the empirical

subtracting assets in the balance sheet of the central bank, and adding its liabilities) we obtain a very similar number, namely 38.1 percent.



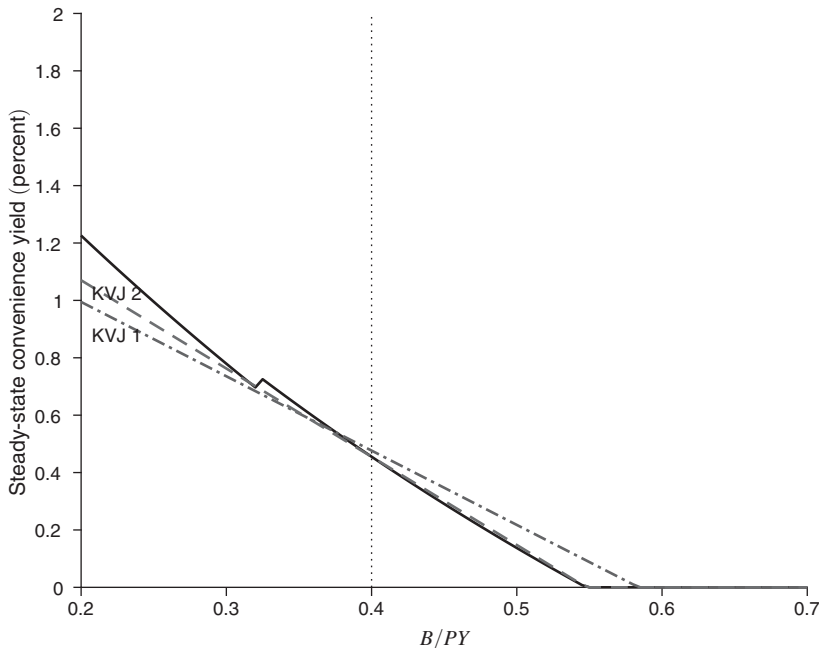


FIGURE 2. TWO-PART KVJ DEMAND CURVE

Notes: The figure plots the steady state convenience yield in the model as a function of the amount of liquidity relative to GDP (solid line) and the regressions line  $CY = b_1 \max\{b_2 - \frac{B}{PY}, 0\}$ , where the estimates of  $b_1$  and  $b_2$  come from the first two columns of Table 3 of Krishnamurthy and Vissing-Jorgensen (2012) (dashed lines). The average value of  $\frac{B}{PY}$  in our sample (40 percent) is indicated by the vertical line.

counterpart of this variable using US Flow of Funds data, and obtain an average of 12.55 percent in our sample.<sup>24</sup>

The remaining targets are chosen to pin down the other steady-state parameters. Loosely speaking, the average real rate of return in the economy (for given convenience yield), the labor share, and the investment to output ratio pin down the discount rate  $\beta$ , the capital share in the production function  $\gamma$ , and the depreciation rate  $\delta$ .<sup>25</sup> Of course, all steady-state parameters affect all targets, so we choose them as to minimize the squared deviations of model implied values from the data—both of which are shown in Table 2. Our calibration yields values of 0.31, 0.79, and 0.01 for  $\phi$ ,  $\theta$ , and  $\chi$ , respectively. Our calibrated value for  $\theta$  is in line with that assumed by many papers using borrowing constraints á la Kiyotaki and Moore (1997). The value for  $\chi$  is smaller than the existing literature on lumpy investment (e.g., Doms and Dunne 1998; Gourio and Kashyap 2007). However, we should stress that we choose to calibrate  $\chi$  using financial data, rather than technological data on lumpy

<sup>24</sup> Section A.1 in the online Appendix describes the details, and Figure A-4 shows the data over our sample.

<sup>25</sup> We target a real interest rate of 2.2 percent, which is in between the average ex post real returns (nominal yield minus realized CPI inflation rate) over the period 1953:I–2008:III on one-year Treasury bills (1.72 percent) and ten-year Treasuries (2.57 percent). The source for the labor share is the Federal Reserve Bank of St. Louis FRED database, while the investment to output ratio is measured from NIPA data, and our notion of investment includes both NIPA investment and durable consumption, consistently with most of the RBC/DSGE literature (e.g., Justiniano, Primiceri, and Tambalotti 2010) and the empirical counterparts in the remainder of the paper.

TABLE 2—TARGETS AND MODEL-IMPLIED VALUES IN LOSS FUNCTION-BASED CALIBRATION OF STEADY-STATE PARAMETERS

Targets	CY	$\frac{\bar{B}}{\bar{PY}}$	Real rate	Liquidity share	Labor share	Investment/GDP ratio
Data	0.455	0.548	2.200	12.55	0.65	0.260
Model	0.455	0.548	2.200	12.55	0.66	0.264

Notes: The table shows the empirical targets and the model-implied values in the loss function-based calibration of the six steady-state parameters. The first two targets are obtained from the regressions in the second column of Table 3 of Krishnamurthy and Vissing-Jorgensen (2012). We set  $CY = b_1 \max\{b_2 - \frac{B}{PY}, 0\}$ , where  $\frac{B}{PY}$  is the average value of government debt in our sample, and  $\frac{B}{PY} = b_2$ . The construction of the liquidity share is described in section A.1 of the online Appendix, and the construction of the remaining three data counterparts—which is standard—is described in footnote 25 of Section IIA. The sample used to compute the data counterparts of the targets is 1953:I–2008:III.

investment, as we broadly consider entrepreneurs as those who are involved in funneling resources from saving to investing agents and face the financing constraint.<sup>26</sup>

As a sanity check on our assumed steady-state value for the convenience yield—and the associated value for  $\phi$ —the left panel of Table A-2 of the online Appendix computes the implied value of the liquidity parameter for a cross section of spreads between pairs of bonds which have almost identical payout and different liquidity. These are the same spreads that we will use in Section IIC to extract a time series of the convenience yield and measure its increase during the crisis (we describe these spreads below in footnote 30 and more in detail in online Appendix A.2). For each security  $j$ , we measure its average spread for the precrisis period using daily data from July 21, 2004 to June, 29, 2007—the common precrisis sample for which we have data for almost all of these securities—and compute its associated degree of liquidity  $\phi^j$  using the steady-state formula derived in online Appendix B.7:

$$(25) \quad 1 - \phi^j = \frac{1 + CY}{CY} \frac{(ytm^{(T,j)} - ytm^{(T,l)}) \beta(1 + CY)}{1 + (ytm^{(T,j)} - ytm^{(T,l)}) \beta(1 + CY)},$$

where  $ytm^{(T,j)}$  and  $ytm^{(T,l)}$  are the steady-state real yields to maturity for zero coupon bond  $j$  with maturity  $T$  and the liquid security of the same maturity.<sup>27</sup> The left panel of Table A-2 shows that for most of these securities, which are relatively liquid, the associated  $\phi^j$  is not far from one. This is what we would expect for instance for short-dated Refcorp bonds, off-the-run Treasury bonds, and high-grade CDS-covered corporate bonds. Longer-dated Refcorp bonds, and especially

<sup>26</sup>Because our entrepreneurs perform both capital and financial investment, it may not be unrealistic that entrepreneurs may not have much time to liquidate private paper before loosing the investment opportunity, and that the fraction of critical entrepreneurs who are financially constrained is small at each point in time. Of course, in a richer setup with technological and financial investment opportunities, an investment function like (14) may be too simplistic. Using a higher value of  $\chi$ , consistent with the literature on lumpy investment, we could still match the KVJ value of the convenience yield as well as the average liquidity share, but we would not longer be able to match the value of the threshold  $\frac{B}{PY}$ .

<sup>27</sup>While our model accommodates only one representative illiquid security, we can price any illiquid security  $j$  whose associated liquidity is  $\phi^j$  as long as its net aggregate supply is small enough that it does not affect the aggregate equilibrium conditions. See footnote 13.

inflation-swapped TIPS, and noncovered Aaa corporate tend to have substantially lower values of  $\phi^j$ .<sup>28</sup>

### B. Parameters Characterizing the Dynamics

The parameters characterizing the dynamics of the model correspond to standard values in the business-cycle literature. We set the constant relative risk aversion (CRRA) parameter  $\sigma$  to 1, the inverse Frisch elasticity of labor supply  $\nu$  to 1, and  $S''(1) = 0.75$  so that the price elasticity of investment is consistent with instrumental variable estimates in Eberly (1997). The average duration of price and wage contracts is four quarters ( $\zeta_p = \zeta_w = 0.75$ ), in line with the recent estimates in Nakamura and Steinsson (2008).<sup>29</sup> We calibrate symmetrically the degree of monopolistic competition in labor and product markets, assuming a steady-state markup of 10 percent ( $\lambda_p = \lambda_w = 0.1$ ), which are commonly assumed values in the literature. Finally, we set the feedback coefficient on inflation ( $\psi_\pi$ ) and the output gap ( $\psi_y$ ) in the interest rate rule (20) to 1.5 and 0.125, respectively—the values in line with the literature that follows Taylor (1993). Transfers slowly adjust to the government net wealth position after intervention ( $\psi_\tau = 0.1$ ) so that government debt finances most of the intervention in the short run and transfers follow a smooth path.

In online Appendix D we study the robustness of our results to alternative values for some of the parameters. As a further check on the reasonableness of our benchmark calibration (and the model), we also consider in online Appendix C the impulse response function of the variables of the model to other shocks often studied in the literature, such as technology, government spending, and conventional monetary policy shocks. Broadly speaking, the effect of these shocks is similar in our model to what has been observed elsewhere in the literature.

### C. Liquidity Shock and Policy Response

We calibrate the size of the post-Lehman crisis liquidity shock from financial data. Because we do not know if any traded security corresponds to our representative illiquid asset, we adopt a strategy that mirrors the one we undertook in the calibration of the steady-state parameters: instead of trying to match a specific spread, we target the change in the convenience yield. Unlike in the case of the steady-state value of  $CY$ , we cannot rely on existing work to obtain a time series of the convenience yield. The remainder of this section describes how we do so. The bottom line is that an arguably conservative estimate of the post-Lehman increase in the convenience yield is 180 basis points. We use this measure to calibrate the size of the liquidity shock.

<sup>28</sup>The reader should bear in mind that there may be measurement issues for any specific security, as well as microstructure factors other than liquidity affecting the average spread, so one should not take the  $\phi^j$ s shown in Table A-2 at face value. For Aaa corporate bond (without CDS cover), for instance, the spread may have a component unrelated to liquidity. In their regression, KVJ indeed obtain a significant positive intercept (equal to 0.347 percent) which may capture the nonliquidity component of the Aaa spread. Note that when constructing the time series of the convenience yield in Section IIC, we address these measurement issues (and other factors, assuming they are security-specific) by taking the principal component.

<sup>29</sup>A lower degree of price rigidities (more in line with the evidence in Bils and Klenow 2004) would deliver the same value for the reduced-form slope of the Phillips curve if we were to incorporate real rigidities in the model.

To be more specific, we take a panel of 18 different financial markets spreads, which differ by assets type and/or maturity, and which the literature argues are mostly—if not solely—driven by liquidity.<sup>30</sup> We measure the extent of their comovement over time, that is, we extract the common factor, using a sample of almost ten years of daily data (from July 21, 2004 to December 31, 2014). We use this sample because it includes data for most of our series, and address the fact that we do not have a fully balanced panel by using a principal component approach that allows for missing observations (Stock and Watson 2002). Figures A-6 and A-7 in the online Appendix show time series of the individual spreads as well as their the projection on the common factor for each spread, and document that for the vast majority of the spreads the common factor captures the bulk of fluctuations following the Lehman episode, except for some shorter-maturity TIPS-Treasury spreads.

The gist of our strategy for measuring the change in the convenience yield rests on the assumption that this common component is proportional to the convenience yield, that is, that  $CY_t = a + bf_t$ , where  $f_t$  is the common factor. This is approximately true in our model, and is a reasonable assumption in the data as well, as long as the spreads we use mostly capture liquidity.<sup>31</sup> Even with the factor at hand, in order to obtain a time series for  $CY_t$  we need to know the parameters  $a$  and  $b$ . We do so by making two assumptions. The first is that the average convenience yield from the beginning of the sample (July 21, 2004) to the very beginning of the financial crisis (June 29, 2007) equals the steady-state value assumed in Section IIA, namely 0.46 percent. The second is that the asset with the highest spread in 2008:IV (this is the BBB CDS-Bond basis) is essentially illiquid at the height of the financial crisis.

<sup>30</sup>The set of spreads includes: (i) The Refcorp/Treasury yield spreads at various maturities (6 months, 1, 2, 3, 4, 5, 7, 10, and 20 year). Longstaff (2004) suggests that the Refcorp/Treasury spread is mostly due to liquidity as Refcorp bonds are effectively guaranteed by the US government, and are subject to the same taxation. (ii) The TIPS-Treasury spreads, which we measure by taking the differences between the constant maturity yield curves for TIPS and Treasury zero-coupon bonds at various maturities (5, 7, 10, and 20 year), adjusting the former using the inflation swap spreads for the same maturities. Fleckenstein, Longstaff, and Lustig (2014) provide evidence of a “TIPS-Treasury bond puzzle,” that is, of differences in prices between Treasury bonds and inflation-swapped TIPS exactly replicating the cash flows of the Treasury bond, and argue that this difference is orders of magnitude larger than the transaction costs of executing the arbitrage strategy. (iii) The CDS-Bond basis spread, constructed as the difference between the yield on corporate bonds whose credit risk is hedged using a credit default swap (CDS) and a Treasury security of equivalent maturity. Bai and Collin-Dufresne (2013) find that measures of funding liquidity are the main drivers of the CDS-Bond basis. Similarly, Longstaff, Mithal, and Neis (2005) find that the nondefault component of corporate spreads (essentially, the CDS-Bond basis) is strongly related to measures of bond-specific illiquidity as well as to macroeconomic measures of bond market liquidity. We do not know the exact maturity of the underlying contracts in each index, but we suspect it is approximately five-year (Choi and Shachar 2013). (iv) The spread between the most recently issued and older 10-year Treasury bonds of the same maturity, called the on-the-run/off-the-run or the bond/old-bond spread, which is a commonly used measure of market liquidity (Krishnamurthy 2002). (v) The Aaa-Treasury spread, which Krishnamurthy and Vissing-Jorgensen (2012) argue is primarily driven by liquidity given the low default rate on Aaa bonds. Section A.2 of the online Appendix provides a detailed description of the data.

<sup>31</sup>In our model, the endogenous variables including the convenience yield are a function of the state variables  $K_t, N_t^g, R_{t-1}L_t, w_{t-1}, \Delta_{t-1}, A_t, \phi_t$  (where  $L_t = B_{t-1}/P_{t-1}$ ,  $w_t = W_t/P_t$ , and  $\Delta_t$  is a distortion measure due to price dispersion—see the online Appendix for details). Because these state variables are either approximately linear function of  $\phi_t$  (such as  $N_t^g$  and  $R_{t-1}L_t$ ), or slow moving ( $K_t, w_{t-1}, \Delta_{t-1}$ ) with constant TFP shock as in our main calibration, the convenience yield is approximately a linear function of  $\phi_t$ . Empirically though it is an open question whether  $CY_t$  and  $\phi_t$  are perfectly correlated—that is, whether spreads follow a one-factor model or a multifactor model, where the other factors capture drivers of the convenience yield that are not related to  $\phi_t$ . In order to address this issue, we estimated a two-factor model. Figures A-8 and A-9 in the online Appendix show that the projections of spreads on the two factors are very similar to those from the one-factor model, suggesting that at least in the sample under consideration using one factor only is reasonable. Finally, the spreads under consideration are associated with different maturities. Online Appendix B.7 shows that under some assumptions the spreads still follow a one-factor model, where the loading on the factor—for given  $\phi^j$ —depends on the maturity of the asset.



FIGURE 3. A TIME-SERIES FOR THE CONVENIENCE YIELD

*Note:* The figure plots a daily time series of the convenience yield from July 21, 2004 to December 31, 2014, constructed using a panel of 18 liquidity-related spreads as described in IIC.

Since the convenience yield is the yield spread between a completely illiquid and a fully liquid security, under this assumption the average of  $CY_t$  in 2008:IV approximately coincides with this spread, and equals 3.42 percent annualized (see online Appendix B.7 for a more formal discussion).

There are two reasons why this value can be viewed as a conservative estimate of  $CY_t$  in 2008:IV. First, even at the height of the crisis the BBB CDS-Bond basis may still have retained some liquidity premium, implying that the convenience yield is higher than its spread. Second, the securities underlying this spread are long term (their maturity is approximately five years), so the spread in 2008:IV should reflect the average expected  $CY_t$  over the duration of the contract, as opposed to the value in that period. To the extent that  $CY_t$  was expected to decline in the following quarters, the value of 3.42 percent is a lower bound.

These two assumptions allow us to translate the common factor into a daily time series of the convenience yield  $CY_t$ , which we plot in Figure 3. Once we have this time series, we can compute the average convenience yield for the pre-Lehman period (that is, the average for 2008:II–III excluding the month of September), which is 1.33 percent. This value suggests that the change in  $CY_t$  due to the Lehman shock was roughly 210 basis points. However, in the weeks preceding the Lehman crisis, the convenience yield had already begun to rise, reaching for instance 1.56 percent on September 1. Therefore, in order to be conservative, we calibrate the size of the shock to achieve an increase of 180 basis point in the convenience yield.<sup>32</sup> The fall

<sup>32</sup> At the other extreme, the overall increase in the convenience yield between the precrisis period and the weeks after Lehman's bankrupt is about 290 basis points annualized. Figure A-15 in the online Appendix compares the

in the resaleability constraint that we obtain—about 70 percent—is broadly consistent with the increase in haircuts after Lehman’s failure documented by Gorton and Metrick (2012).

We choose the persistence of the shock  $\rho_\phi = 0.953$  so that the implied expected duration of the ZLB episode is six quarters. This value falls close to the midpoint between survey evidence of market participants (Moore 2008) and the predictions of an estimated interest rate rule (Rudebusch 2009). Later, we present results based on expectations of more severe financial disruption.

Finally, the parameter  $\psi_k$  is calibrated to generate a government intervention of about \$1.4 trillion (10 percent of GDP), consistent with the increase in the asset side of the Fed’s balance sheet after the collapse of Lehman Brothers, as displayed in Figure 1.<sup>33</sup>

### III. Results

#### A. Simulating the Financial Crisis: The Impact on Macroeconomic and Financial Variables

Figure 4 shows the response of output, inflation, and the nominal interest rate to the calibrated liquidity shock  $\phi_t$  in the model, and compares it to the dynamics in the data during the Great Recession. Specifically, the right-hand column plots the predicted path of variables for 16 quarters, conditional on the shock hitting at the beginning of the first period under perfect foresight. The left-hand column shows the changes in the data also for 16 quarters (i.e., until 2012:III) relative to 2008:III, when the Lehman bankruptcy occurred. We measure output as the log of the sum of consumption and investment from the NIPA tables. We report the percentage deviation from a linear trend estimated from 2000:I to 2012:III, normalized to zero in 2008:III. For inflation, we use the annualized percentage change in the GDP deflator, and express it in deviation from the 2 percent inflation long-run objective of the Fed. The nominal interest rate is the effective federal funds rate.

The liquidity shock explains a large component of the response of the macroeconomy to the Lehman episode. The model explains more than 50 percent of the output reduction (−4.4 percent in the model versus −7.8 percent in the data); it also accounts for a 2.5 percent drop in the inflation rate, which corresponds to the entire fall of inflation relative to target in the data, and to three-quarters of the change from

response of macroeconomics and financial variables to this larger shock with the baseline case.

<sup>33</sup>We include currency swaps with foreign central banks in computing the size of the intervention. The rationale for this choice lies in the fact that a key purpose of the currency swaps was to provide dollar liquidity to foreign banks that needed funding for dollar-denominated assets, as discussed in Fleming and Klagge (2010). While it is hard to know for sure what these dollar-denominated assets represented, arguably they were mostly claims originated in the United States, such as mortgage-backed securities. We exclude however many other important policy during this period, such as expansion of FDIC insurance, Temporary Liquidity Guarantee Program, and Federal Home Loan Bank System Loan Facilities. We do so to stay on the conservative side in our counterfactual experiment. Because we calibrate the size of liquidity shock to the increase of the convenience yield observed in the data, the difference between intervention and no intervention would be larger with a larger size of the intervention. The second reason for not incorporating these policies into our analysis is that they are harder to quantify as they largely consist in providing insurance rather than the actual liquidity injections done by the central bank, which we can measure in the data. Moreover, our framework is best suited to analyze the effects of policies which directly change the compositions of private holdings of assets of different liquidity. Our framework has less to say about policies that may indirectly improve the working of private financial intermediaries.

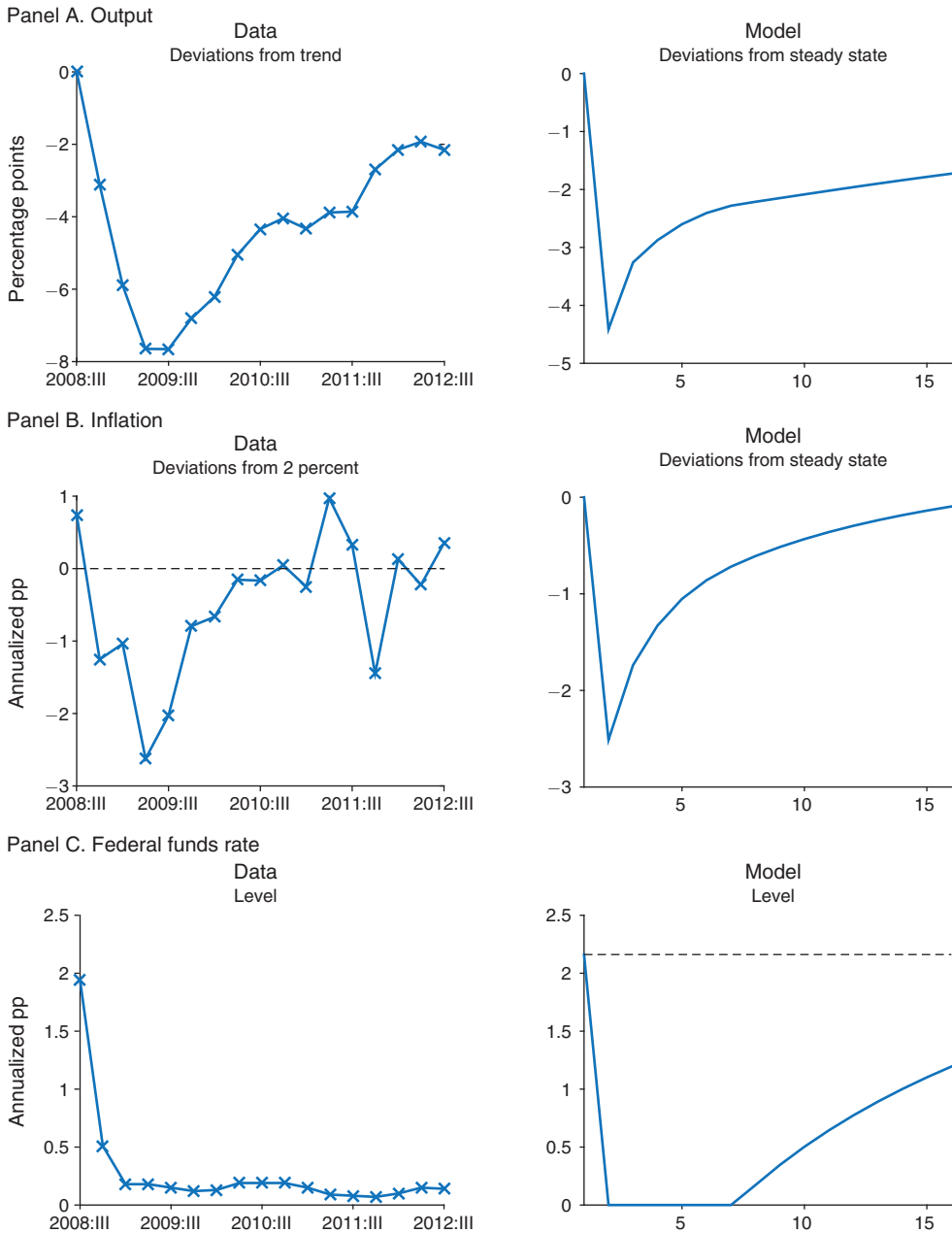


FIGURE 4. RESPONSE OF OUTPUT, INFLATION, AND THE NOMINAL INTEREST RATE TO THE LIQUIDITY SHOCK

*Notes:* The figure compares the evolution of output, inflation, and the nominal interest rate in the data (left column) and in the model in response to the calibrated liquidity shock (right column). The data start in 2008:III. Both data and model are plotted for 16 quarters. Output in the data (panel A) is the sum of consumption and investment, in percentage log deviations from a linear trend estimated from 2000:I to 2012:III, and is normalized to zero in 2008:III. Inflation in the data (panel B) is the annualized quarterly inflation rate of the GDP deflator. The interest rate in the data (panel C) is the annualized effective Federal Funds Rate. Output in the model (panel A) is the log deviation from steady state in percentage points. Inflation in the model (panel B) is expressed in annualized percentage points. The interest rate in the model (panel C) is the annualized level of the nominal interest rate in percentage points (the horizontal line is its steady-state value).

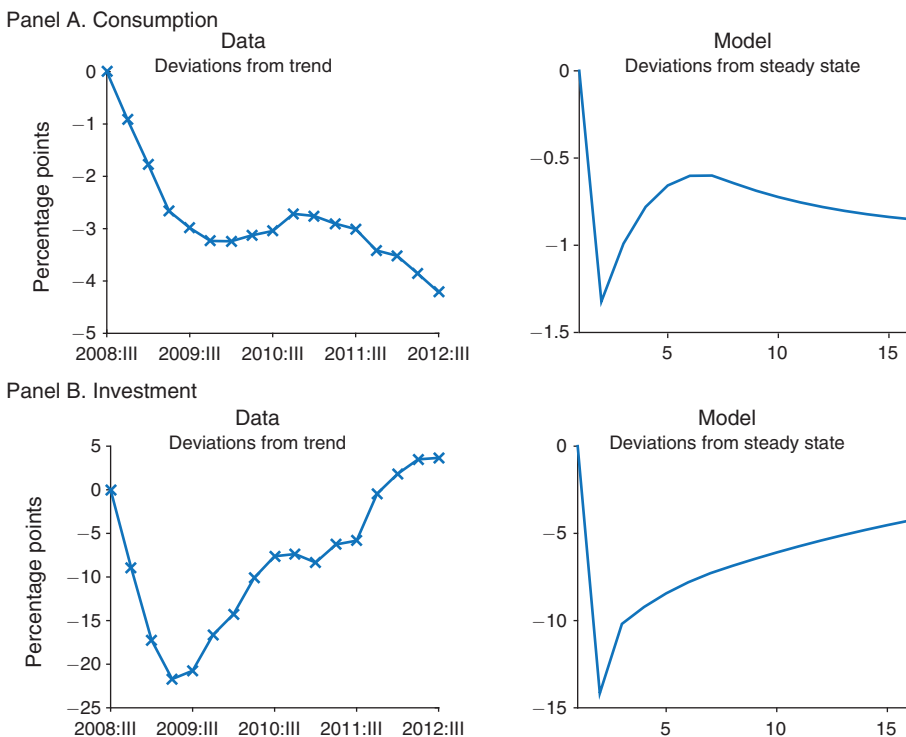


FIGURE 5. RESPONSE OF CONSUMPTION, INVESTMENT, THE NOMINAL VALUE OF CAPITAL, AND CONVENIENCE YIELD TO THE LIQUIDITY SHOCK

(Continued)

its value in 2008:III; finally, it shows the nominal interest rate hitting the zero lower bound following the crisis and remaining there for a considerable period. Note that the model expects the recovery of real activity after the shock to be sluggish, which was indeed the case in the data.

Panels A and C of Figure 5 show the decomposition of the output drop in the relative contribution of consumption (panel A) and investment (panel B) in the model and in the data.<sup>34</sup> The model explains about two-thirds of the actual fall in investment (−14.2 percent versus −22.3 percent), and almost one-half of the fall in consumption (−1.3 percent versus −3.0 percent). The model underpredicts the fall investment, possibly because of the absence of an explicit residential sector. Nevertheless, the broad empirical patterns are correct, in that investment drops substantially more than consumption in percentage terms both in the model and the data.

Panel C of Figure 5 shows the behavior of the convenience yield  $CY_t$ , which is the quarterly average of the time series shown in Figure 3 and is expressed in deviations from the KVJ steady-state value of 0.46 percent, and the total nominal value of capital (panel D), measured in the data using the Flow of Funds (see online

<sup>34</sup>Our empirical counterpart of consumption excludes durable goods, which instead we treat as part of investment, consistently with much of the literature (Justiniano, Primiceri, and Tambalotti 2010). As for output, both the variables are measured in logs, and are shown in percentage deviation from a linear trend estimated from 2000:I to 2012:III (separately estimated for each variable), and are normalized to zero in 2008:III.



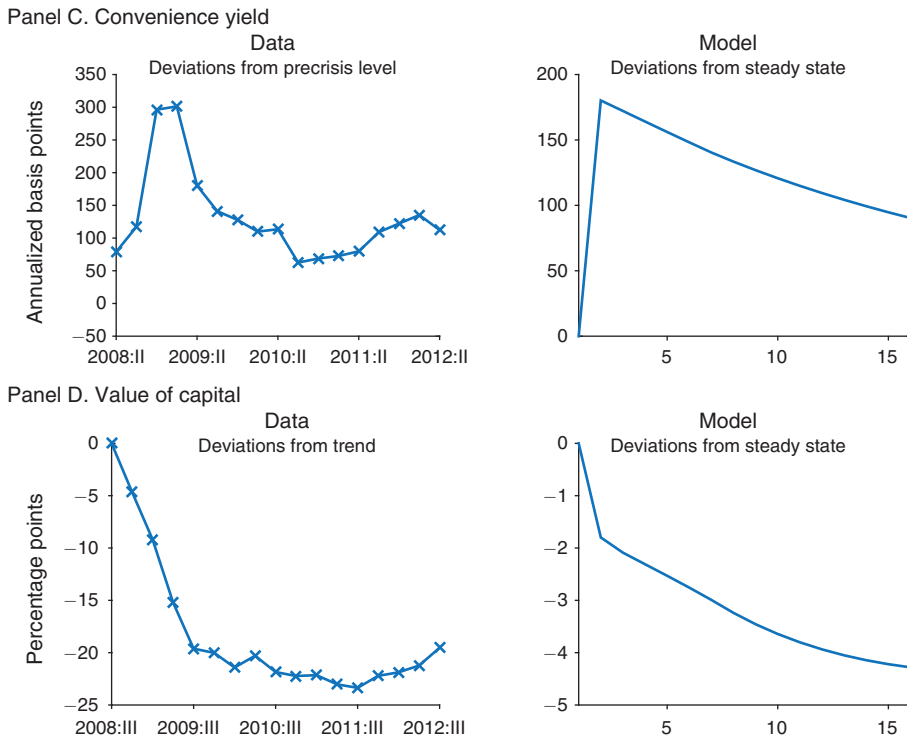


FIGURE 5. RESPONSE OF CONSUMPTION, INVESTMENT, THE NOMINAL VALUE OF CAPITAL, AND CONVENIENCE YIELD TO THE LIQUIDITY SHOCK (Continued)

*Notes:* The figure compares the evolution of consumption, investment, nominal value of capital, and convenience yield in the data (left column) and in the model in response to the calibrated liquidity shock (right column). The data start in 2008:III. Both data and model are plotted for 16 quarters. Consumption in the data (panel A) is total consumption minus durable consumption. Investment in the data (panel C) is investment plus durable consumption. The nominal value of capital in the data (panel D) is the value of illiquid assets from the flow of funds as defined in the text. These three variables are expressed in percentage log deviations from a linear trend estimated from 2000:I to 2012:III, and are normalized to zero in 2008:III. The convenience yield in the data (panel B) is in annualized basis points (its computation is described in Section IIB). Consumption (panel A), investment (panel C), and the nominal value of capital (panel D) in the model are log deviations from steady state in percentage points. The convenience yield in the model (panel B) is the annualized absolute deviation from steady state expressed in basis points.

Appendix A.1) and in the model as  $P_t q_t K_t$ .<sup>35</sup> By construction, the rise in  $CY_t$  in the model matches the change in the convenience yield between the pre-Lehman period and the 2008:IV average. In the data  $CY_t$  rises again between 2008:IV and 2009:I, and then falls faster than the model would have predicted in the second half of 2009, possibly because of a number of other factors and policy interventions (e.g., the stress test and the first round of large-scale asset purchases) that are not incorporated in the model. Bear in mind that the model impulse responses capture *ex ante* expectations as of 2008:IV, while the data measure *ex post* outcomes. We should also recognize that our deterministic simulations are set to match the modal expectations of the duration

<sup>35</sup>The convenience yield is computed as the spread  $\overline{CY}_t$  (the spread between a perfectly illiquid and a perfectly liquid bond: see the discussion in Section IB), and is expressed in annualized basis points. The value of capital is measured in logs, and like the other variables is shown in percentage deviation from a linear trend estimated from 2000:I to 2012:III, normalized to zero in 2008:III.

of the ZLB as of 2008:IV (six quarters), but do not capture the uncertainty concerning the expected duration of the crisis, which was pervasive.

The model can only account for about one-fifth of the observed decline in the value of capital.<sup>36</sup> Shi (2015) discusses the reason why, in the absence of other frictions, a liquidity shock in the KM model generally leads to a *rise* in the real value of equity. As the resaleability constraint tightens, the demand for assets increases relative to the supply (including the equity with limited resaleability), which tends to push up equity prices *ceteris paribus*. Our results indicate that incorporating nominal frictions and the ZLB does generate a fall in the value of equity, even though such a fall is smaller than observed in the data. One way in which this limitation could be addressed is to explain the liquidity shock endogenously. Cui and Radde (2014) embed a search-and-matching framework into the KM model and argue that this approach addresses Shi's critique.<sup>37</sup>

In short, our simulated crisis generates movements in macroeconomic variables following a liquidity shock that are not far from their empirical counterparts following Lehman's bankruptcy. Apart from the insufficient drop of equity prices, the model does not fully account for two aspects of the data, which we believe are related. The first is that the model only explains a little bit more than one-half of the observed fall in output. The second is that in the model, the nominal interest rate starts increasing six quarters after the onset of the shock, while in the data the duration of the ZLB was much longer.

Obviously, several other shocks played an important role in the crisis in addition to the negative shock to the liquidity of private paper, such as the debt-deleveraging process at the household level, studied theoretically in Eggertsson and Krugman (2012) and documented empirically in Mian and Sufi (2014), or slow-moving secular factors (e.g., Eggertsson and Mehrotra 2014). These additional forces can account for both the drop in output our model does not explain, as well as the delay in the interest rate liftoff in the data relative to our model's forecast, which is only conditioned on the shock to the liquidity of private paper. Our paper only focuses on the macroeconomic consequences of the disruption in the financial system following Lehman's bankruptcy, and on the effect of the Federal Reserve's policies to mitigate such a disruption.

### B. *The Great Escape? What Would Have Happened in the Absence of the Liquidity Facilities?*

What would have happened after the liquidity shock in the absence of unconventional policy? This is the central question of the paper, which we can address using our model with liquidity constraints. The left panel of Figure 6 shows the gain in output and inflation in the baseline scenario due to the intervention. The model suggests that, without the facilities, the drop in output would have been significantly larger, -5.8 percent instead of -4.4 percent, that is, the output contraction

<sup>36</sup>The model predicts the real value of capital  $q_t$  to fall, as shown in Figure A-10 in the online Appendix. The figure shows that nominal rigidities and the ZLB are essential for this result.

<sup>37</sup>Other natural candidates include mechanisms that relate the fall in resaleability to a concurrent drop in current or expected future total factor productivity. See Guerron-Quintana and Jinnai (2015).

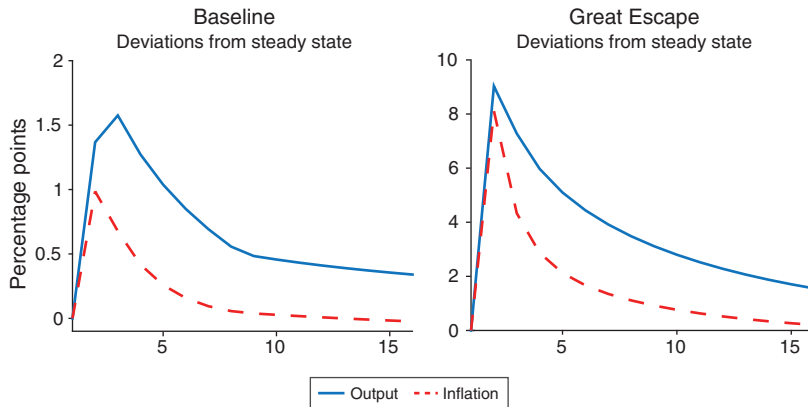


FIGURE 6. THE EFFECT OF THE LIQUIDITY FACILITIES ON OUTPUT AND INFLATION IN THE BASELINE AND IN THE GREAT ESCAPE EXPERIMENT

*Note:* The figure shows the difference between counterfactual and actual response of output (solid line) and inflation (dashed line) in the model in response to the calibrated liquidity shock under the baseline persistence (left panel), and with increased persistence such that the zero lower bound binds for 20 quarters (right panel).

would have been 30 percent more severe in the absence of the intervention. In addition, inflation would have declined by almost 3.5 percentage points, compared to 2.5 with intervention. Figure 6 also makes the point that looking at the first period understates the importance of unconventional policy. Given our assumption that, on impact, the facilities do not relax the entrepreneurs' resaleability constraint, entrepreneurial investment cannot avoid the direct hit due to the fall in resaleability. The policy effect in the first period is still significant because it affects asset prices and consumption through expectations. From the second period onward, the effect is larger, as the policy changes the aggregate amount of liquidity in the economy by changing the household portfolio toward the liquid asset.

The effect of the liquidity facilities on the convenience yield is not negligible (45 basis points annualized: see Figure A-12 in the online Appendix), but smaller as a fraction of the initial response than in the case of the macro variables. Much of the early literature on the effect of the facilities focused on the reduction in spreads as the main metric to interpret their success (McAndrews, Sarkar, and Wang 2008; Taylor and Williams 2009). Our model suggests that this metric may not be entirely appropriate. Even if the reduction in spreads is limited, the macroeconomic impact is substantial. In the model, not only is the private sector better off because of the liquidity injection, but the government actually ends up making money off the transaction: \$27 billion in the first year in our baseline calibration.<sup>38</sup>

In the baseline scenario, we calibrate the persistence of the shock assuming that the private sector expected the ZLB to bind for six quarters right after Lehman's bankruptcy. Yet, given the intensity of the crisis, and the degree of disruption in financial markets, the Great Recession has often been compared to previous financial crises, such as the Great Depression and Japan's "Lost Decades." These episodes,

<sup>38</sup>Federal Reserve transfers to the US Treasury (profits minus operating expenses) reached two consecutive records in 2009 (\$47.4 billion) and 2010 (\$78.4 billion), largely as a result of the increased interest income on security holdings.

also characterized by downward pressure on prices and zero nominal interest rates, lasted much longer than six quarters.

To capture the possibility that the public had expected a Depression-like crisis, we consider the same shock but increase its persistence, so that the ZLB binds for 20 quarters (5 years). The right panel of Figure 6 shows the gain in output (solid) and inflation (dashed) due to the intervention in this alternative scenario, calibrating the size of the intervention as before at \$1.4 trillion. Without the intervention, the drop in output (almost 20 percent) and inflation (about 15 percent) is of an order of magnitude not seen in the United States since the Great Depression. In this case, thus, unconventional credit policy becomes much more effective. The policy response cuts the losses in output and inflation by roughly one-half—generating a recession of similar order as seen in the data.

This “divine coincidence” (Christiano, Eichenbaum, and Rebelo 2011), according to which the policy intervention becomes more effective as the economy approaches the “disaster area,” represents an element of commonality with the literature on the multiplier of government spending in a liquidity trap (see also Eggertsson 2011). A key reason for the effectiveness of the policy intervention is the assumption of price rigidities and the presence of the ZLB. In the absence of these two frictions, the intervention would have substantially less effect, as shown in Figure A-14 in the online Appendix, which shows the increase in output as a result of the policy under different assumptions. With flexible prices, the intervention is almost irrelevant while in the absence of the ZLB, traditional monetary policy (via interest cuts) largely substitutes unconventional policy, hence making it much less necessary. We clarify the logic for these results in the next two sections.

Finally, in online Appendix D we consider several perturbation of the baseline parameters to explore the sensitivity of the results. The overall tenor of the results remain unchanged: the liquidity shock generates a recession, and the liquidity facilities are effective in mitigating the consequences of the shock.

### *C. The Role of Nominal Frictions*

The previous two sections showed that the KM liquidity shocks can rationalize the behavior of macroeconomic and financial variables during the Great Recession, and that unconventional credit policy might have prevented an even larger downturn. The next two sections shed some light on the ingredients behind our main results. We start from the role of nominal rigidities. Absent this friction, liquidity shocks would only affect the composition of output, decreasing investment and increasing consumption, but would have had very little effect on aggregate activity.

The four panels of Figure 7 show the response of output, investment, consumption, and the real interest rates with (solid) and without (dashed) nominal rigidities under the baseline calibration. For simplicity, but also to magnify the differences, we show the responses without policy intervention. The top left panel of Figure 7 shows that, with flexible prices and wages, the response of output is indeed very small, even though the liquidity shock has still a large impact on investment (top right panel). The equilibrium condition for investment (14) shows that when  $\phi_t$  falls the amount of resources available to entrepreneurs for investment drops, regardless of nominal rigidities. Clearly, the financial frictions are driving the fall in investment. Nominal

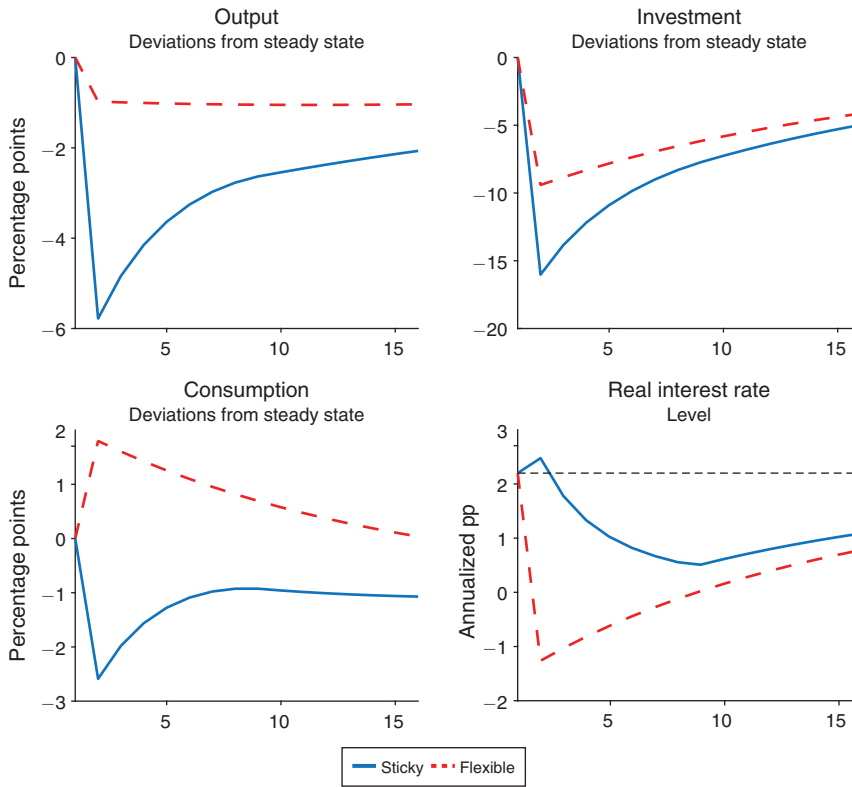


FIGURE 7. THE ROLE OF NOMINAL RIGIDITIES

*Note:* The figure compares the response of output (top left), investment (top right), consumption (bottom left), and the real interest rate (bottom right) to the liquidity shock under the baseline calibration in the absence of intervention with (solid line) and without (dashed line) nominal price and wage rigidities.

frictions exacerbate the effect of the shock by depressing current and future economic activity and therefore equity prices. This channel explains why quantitatively the response of investment is larger with nominal rigidities, but qualitatively the two impulse responses are similar.

Conversely, consumption moves in opposite directions depending on whether prices and wages are flexible (bottom left panel). Consumption rises under flexible prices and wages, instead of falling as in our simulation with nominal rigidities. Intuitively, consumption needs to make up for the drop in investment since, in that case, output does not drop as much without nominal frictions. The reason for a small response of output absent nominal rigidities is that the liquidity shock only affects the accumulation of the capital to be used for production in the future, but has no effect on either productivity or the existing capital stock. Output would drop substantially only if, for some reason, labor were to be used much less intensively for production. If prices are flexible and the elasticity of labor supply is not too extreme, however, the effect on hours is not very pronounced. Hence, aggregate output remains more or less unchanged.

The mechanism of adjustment hinges upon the behavior of the real interest rate. To get households to spend more, the real interest rate needs to decline. The bottom right panel of Figure 7 shows that the real interest rate absent nominal frictions

(the so-called natural rate of interest) becomes negative in response to the liquidity shock, so that consumption rises.<sup>39</sup> This fall in the real interest rate is hard to achieve, however, when prices are rigid. With some (but not full) price flexibility, the private sector starts expecting some deflation in future periods when the shock is still perturbing the economy, while the Taylor rule implies zero inflation as soon as the shock is over. The interaction of the ZLB and price frictions leads to higher real interest rates owing to expected deflation, which causes consumption to fall with investment. The longer the private sector expects the shock to last, the stronger deflation is, and hence the rise in real rates. The fact that the liquidity shock cannot generate much effect if all prices are flexible is an important quantitative findings of this paper.

#### D. The Zero Lower Bound

Given the relevance of nominal rigidities stressed in the previous section, not surprisingly conventional monetary policy also plays an important role in our results. But the presence of the ZLB impairs full monetary policy stabilization.

Figure 8 shows the response of output, the nominal interest rate, and the real interest rate ignoring the ZLB constraint, with (solid) and without (dashed) the liquidity facilities. In order to show that the ZLB works as an amplification mechanism for the liquidity shock, let us first focus on the case without intervention—that is, the dashed lines. As we have seen in Figure 6, output drops by almost 6 percent without intervention when the ZLB is binding. In the absence of the ZLB, even without intervention, output would have fallen only by one-half of that amount. The reason is that, in this case, a monetary authority following the Taylor rule (20) would have lowered the nominal interest rates below zero, thereby inducing a fall in the real interest rate from 2.2 percent (the steady state) into negative territory.

In contrast, under the ZLB the nominal interest rate is stuck at zero. The zero bound amplifies the effect of the liquidity shock not only because the constraint is binding in a given period, but especially because agents expect it to be binding in the future. This belief lowers expected future income and generates deflationary expectations. Such expectations lead to a rise in real rates (shown in Figure 7) and a decline in demand. In this situation, unconventional policy stimulates demand by changing the portfolio composition of the private sector, thereby enabling entrepreneurs to pursue more investment opportunities. The impact of the policy on investment supports demand in all periods when the economy is in a crisis, indirectly boosting consumption via its effect on inflation expectations, and hence lowering the real rate. In this sense, unconventional policy can substitute for interest rate policy when the latter is hindered by the ZLB.<sup>40</sup> Yet, the actual liquidity facilities (as per our calibration) are less than a perfect substitute. At the ZLB, the size of the liquidity intervention necessary to achieve the same output response to the crisis as

<sup>39</sup> We note in passing that in our framework financial frictions have a direct effect on the natural rate of interest via the convenience yield, as equation (16) highlights. The relationship between liquidity and the natural rate of interest is a potentially important one for monetary policy. We leave its analysis for future research.

<sup>40</sup> The Great Escape calibration forcefully illustrates the role of expectations in determining the effectiveness of unconventional policy, as it shows that unconventional policy becomes very effective when ZLB is expected to be binding for a long time.

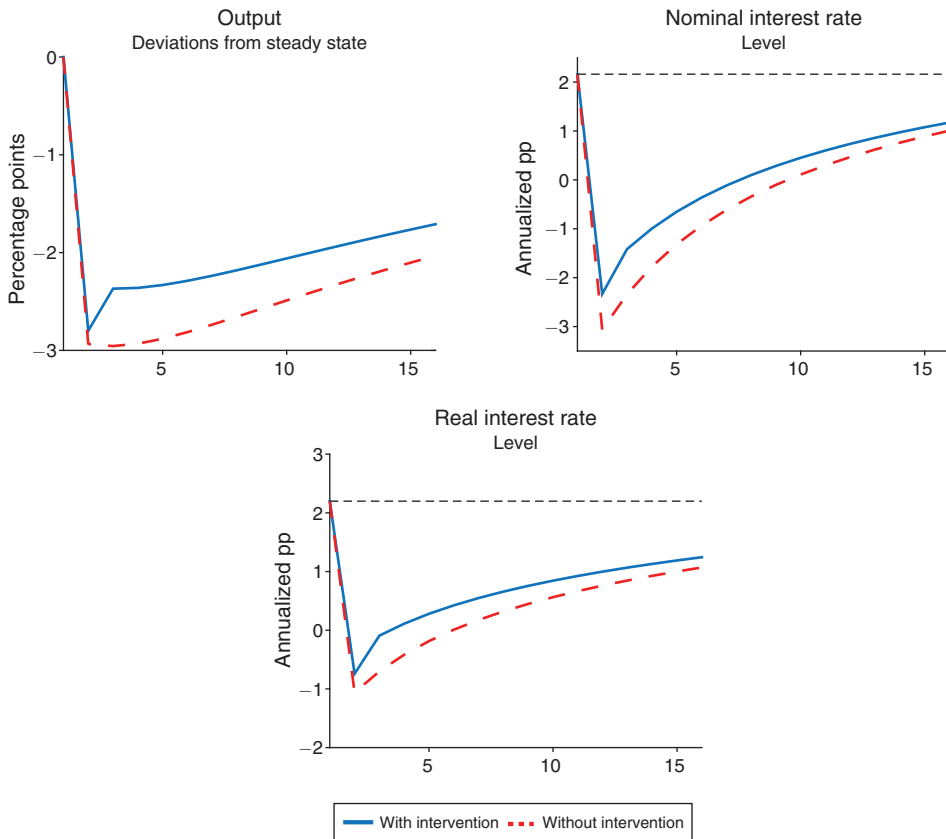


FIGURE 8. THE ROLE OF THE ZERO LOWER BOUND

*Note:* The figure compares the response of output (top left), nominal interest rate (top right), and real interest rate (bottom) to the liquidity shock under the baseline calibration when the zero lower bound on the nominal interest rate is ignored with (solid line) and without (dashed line) intervention.

when the nominal interest rate can go negative is almost 30 percent of GDP—three times more than the baseline liquidity injection (see online Appendix Figure A-13).

If the ZLB is not binding, unconventional policy is much less needed, simply because conventional policy can do its job in boosting demand. Indeed, Figure 8 shows that the paths of output with and without unconventional policy are not very different when the ZLB is not binding.

#### IV. Conclusions

In this paper, we have proposed an analysis of the economic and financial crisis of 2008 based on shocks to the liquidity of private paper. We have incorporated a set of financial frictions into a standard DSGE model to show that the Federal Reserve's liquidity facilities made a material difference in preventing the recession from becoming deeper, substituting for the conventional interest rate policy that was constrained by the zero lower bound. Had market participants in 2008 expected the zero lower bound to last for as long as it did, the Fed may have prevented the Great

Recession from becoming a second Great Depression, although this hypothesis is admittedly extreme. Our analysis does not deny the importance of other shocks in explaining the crisis nor the importance of other policy intervention, such as fiscal policy.

Our results rely on the crucial distinction that the government can issue perfectly liquid papers while the private sector cannot. The ability of governments to issue fiat currency and raise taxes provides a rationale for this assumption. If government bonds become subject to default risk and sensitive to information on a possible default, also their liquidity would become much less than perfect, as in the recent cases of Greece, Portugal, and Ireland. In this case, the government has only limited ability to conduct unconventional credit policy and the expectations about future fiscal policy would affect both the valuation and the liquidity of government bonds. We leave this topic for future research.<sup>41</sup>

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<sup>41</sup> We have also abstracted from the wealth distribution across heterogeneous agents by assuming complete sharing of consumption and assets among family members at the end of every period. Absent this pooling of resources, the distribution of net worth across heterogeneous producers and consumers affects aggregate production and asset prices as in Bernanke and Gertler (1989) and Kiyotaki and Moore (1997). Because the balance sheet takes time to adjust, the recovery of aggregate production may be slow after a large financial crisis. In such an economy, the government purchase of illiquid private paper with government paper may not be enough to avoid a deep and prolonged recession.



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